Day 03

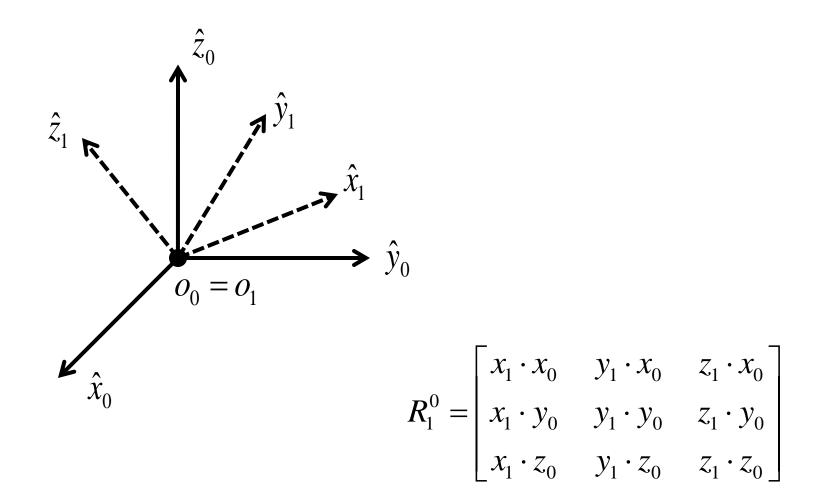
Rotations

1/17/2011

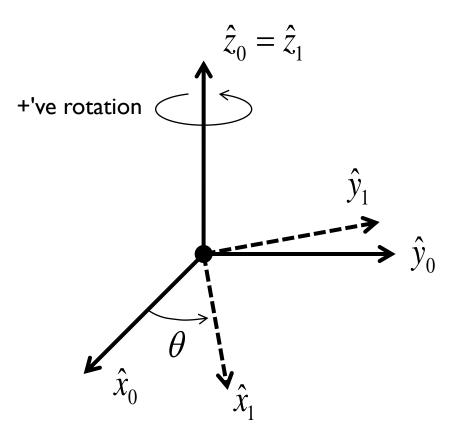
Properties of Rotation Matrices

- $R^T = R^{-1}$
- the columns of R are mutually orthogonal
- each column of R is a unit vector
- det R = 1 (the determinant is equal to 1)

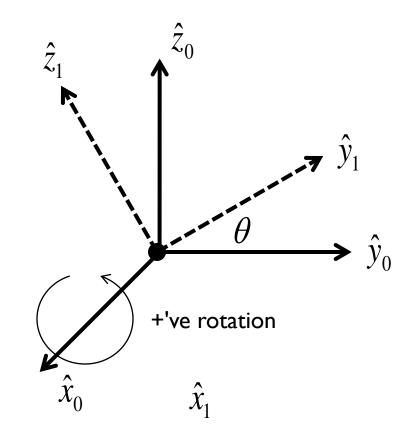
Rotations in 3D



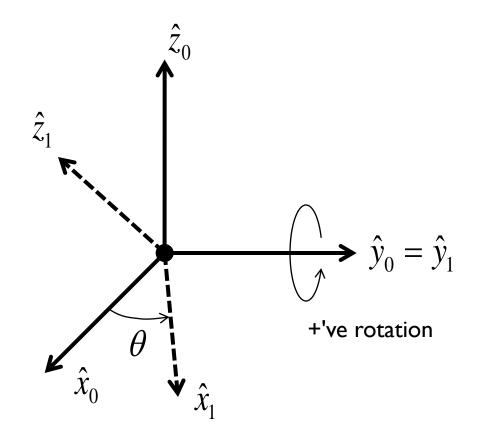
Rotation About z-axis



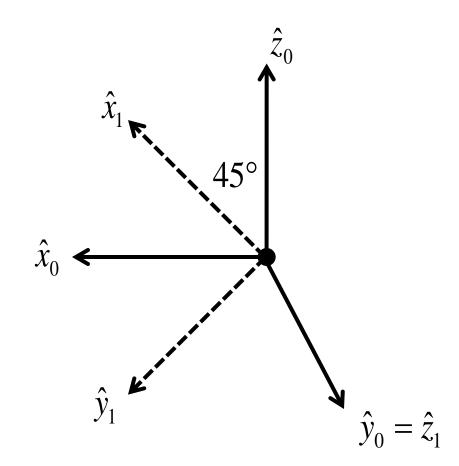
Rotation About x-axis



Rotation About y-axis



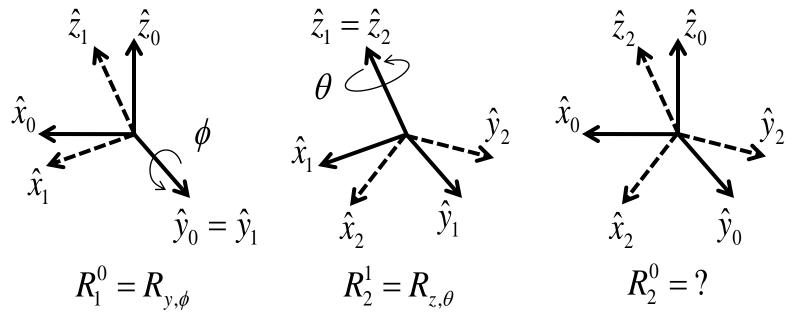
Relative Orientation Example



Successive Rotations in Moving Frames

- 1. Suppose you perform a rotation in frame $\{0\}$ to obtain $\{1\}$.
- 2. Then you perform a rotation in frame $\{1\}$ to obtain $\{2\}$.

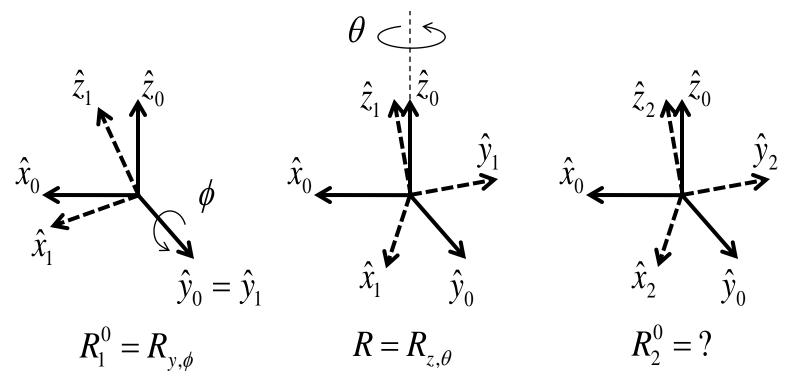
What is the orientation of {2} relative to {0}?



Successive Rotations in a Fixed Frame

- I. Suppose you perform a rotation in frame {0} to obtain {1}.
- 2. Then you rotate $\{1\}$ in frame $\{0\}$ to obtain $\{2\}$.

What is the orientation of {2} relative to {0}?



Composition of Rotations

- I. Given a fixed frame {0} and a current frame {1} and R_1^0
 - if $\{2\}$ is obtained by a rotation R in the *current frame* $\{1\}$ then use postmulitplication to obtain:

$$R = R_{2}^{1}$$
 and $R_{2}^{0} = R_{1}^{0}R_{2}^{1}$

- 2. Given a fixed frame {0} and a frame {1} and
 - if $\{2\}$ is obtained by a rotation R in the fixed frame $\{0\}$ then use premultiplication to obtain:

$$R_2^0 = RR_1^0$$

Rotation About a Unit Axis

